

$$\frac{d^n z^e}{dz^n} = \frac{\Gamma(e+1)\Gamma(-n)}{\Gamma(e-n+1)\Gamma(-n)} = \frac{z^{e-n}}{\Gamma(-n)} \mathbf{B}(e+1, -n)$$