

$$\frac{d^{\mu}\frac{1}{x}}{dx^{\mu}}=\int_0^{\infty}(-1)^{\mu}e^{-ax}a^{\mu}da=\frac{(-1)^{\mu}\Gamma(\mu+1)}{x^{1+\mu}}$$