

$$\frac{dN_i}{dt} = Y_i + N_{i-1}(t)\gamma_{i-1} - N_i(t)\beta_{i-1}$$